

Code: MEMD1T4

**I M.Tech - I Semester – Regular/Supplementary Examinations –
January - 2017**

**FINITE ELEMENT METHODS
(MACHINE DESIGN)**

Duration: 3 hours

Max. Marks: 70

Answer any FIVE questions. All questions carry equal marks

1. Determine the deflection at the centre of a simply supported beam of span length l subjected to uniformly distributed load w /unit length throughout its length as shown in Figure-1 using Rayleigh-Ritz method. Take the flexural rigidity, EI is constant for the beam. 14 M

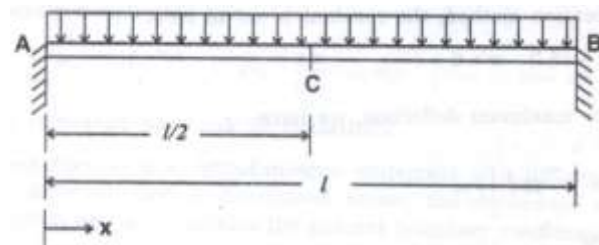
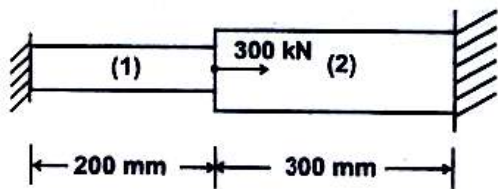


Figure-1

2. An axial load of 300 kN is applied at 20°C to the rod as shown in Figure-2. The temperature is then raised to 60°C .

Determine:

- | | |
|------------------------------------|-----|
| a) Nodal displacements | 6 M |
| b) Reaction forces at the support. | 4 M |
| c) stresses in elements | 4 M |



Aluminum	Steel
$E_1 = 70 \text{ GPa}$	$E_2 = 200 \text{ GPa}$
$A_1 = 900 \text{ mm}^2$	$A_2 = 1200 \text{ mm}^2$
$\alpha_1 = 23 \times 10^{-6} / ^\circ\text{C}$	$\alpha_2 = 12 \times 10^{-6} / ^\circ\text{C}$
$L_1 = 200 \text{ mm}$	$L_2 = 300 \text{ mm}$

Figure-2

3. a) Derive the stiffness matrix for the truss element. 9 M

b) Briefly discuss about the effect of temperatures on truss element. 5 M

4. A beam fixed at one end and supported by a roller at the other end, has a 20 kN concentrated load applied at the center of the span, as shown in Figure-3. Calculate the deflection under the load and support reactions. 14 M

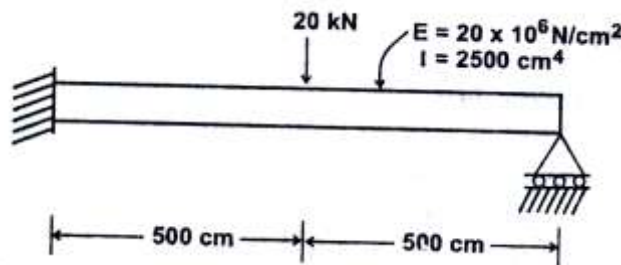


Figure-3

5. Compute the strain-displacement matrix for the element show in Figure-4. Also determine the element strains. Take

$u = [0 \ 0 \ 2 \ 1 \ 0 \ -1]^T$. All quantities are in mm.

14 M

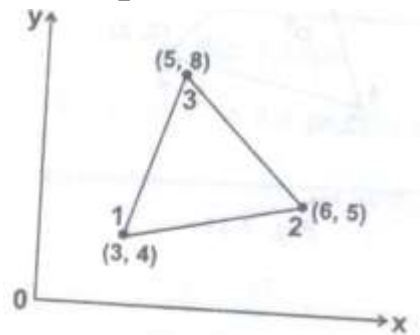


Figure-4

6. a) Evaluate the following integral using one point and two point Gauss Quadrature. Compare this with exact solution.

10 M

$$\int_{-1}^1 \left[3e^x + x^2 + \frac{1}{x+2} \right] dx$$

b) Differentiate sub-parametric and super-parametric elements.

4 M

7. Determine the Eigen values and Eigen vectors for stepped bar shown in Figure-5. Take $E = 200\text{GPa}$ and Specific density $\rho = 7000 \text{ kg/m}^3$

14 M

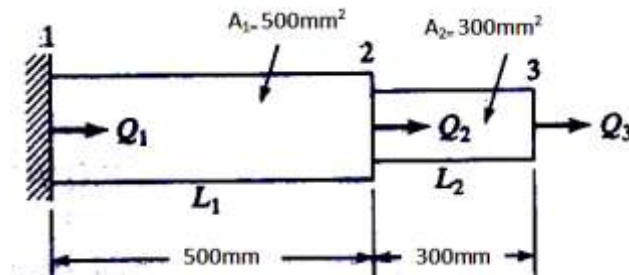


Figure-5

8. Explain the following:

- a) h-refinement and p-refinement 4 M
- b) Complete and incomplete interpolation functions. 4 M
- c) Convergence requirements 6 M